Fuzzy Clustering Using Automatic Particle Swarm Optimization

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Abstract—Fuzzy clustering is a popular unsupervised learning method used in cluster analysis which allows a data point to belong to two or more clusters. Fuzzy c-means is one of the most well-known and used methods, however, the number of clusters need to be defined in advance. This paper proposes a clustering approach based on Particle Swarm Optimization. This approach automatically determines the optimal number of clusters using a threshold vector that is added to the particle. The algorithm starts by partitioning the data set randomly within a preset maximum number of clusters in order to overcome the fuzzy c-means shortcoming of the predefined cluster count. A reconstruction criterion is applied to evaluate the performance of the clustering results of the proposed algorithm. The experiments conducted show that the proposed algorithm can automatically find the optimal number of clusters.

Keywords—Fuzzy Clustering, Particle Swarm Optimization (PSO), data mining

I. INTRODUCTION

Data mining is called exploratory data analysis, among other things. It is an analytic process designed to explore data. Data mining aims to search for consistent patterns or systematic relationships between variables. It then validates the findings by applying the detected patterns to new subsets of data [1]. It is a statistical analysis process which can identify the clusters along with collection of data. Data mining can be achieved by classification, association, prediction, sequential pattern, similar time sequences and clustering [2].

Clustering analysis is one of the popular approaches and has been widely used in data mining. Clustering analysis is a process to identify groups or clusters based on some similarity measures. Most clustering algorithms can be categorized into two popular techniques known as hierarchical and partitional clustering. The output of the hierarchical clustering is a tree showing a sequence of clusters with each cluster being a partition of the data set. Hierarchical clustering does not specify the number of clusters, and the output is independent of the initial condition. However, the hierarchical clustering is static, i.e., the data points assigned to a cluster cannot be reassigned to another cluster. In addition, it will fail to separate overlapping clusters due to the lack of information regarding the global shape or size of the clusters. On the other hand, partitioned clustering requires a fixed number of clusters to be specified a priori. Objective functions such as square error function are used as a criteria in the optimization process of data partitioning. Partitioned clustering uses an iterative process to optimize the cluster centers, as well as the number of clusters. However, it is a challenge to find the “optimum” number of clusters since it always requires prior knowledge about the data. The advantages of hierarchical algorithms are the disadvantages of the partitional algorithms and vice versa.

The goal of clustering involves the task of dividing data points into homogeneous groups such that the data points in the same group are as similar as possible and data points in different groups are as dissimilar as possible [3], [2]. The importance of clustering is documented in pattern recognition [4], machine learning, image analysis [5], information retrieval, etc. Depending on whether a data point belongs to a single cluster or several clusters with different membership degrees, clustering methods can be categorized as either hard clustering [6], [7] or fuzzy clustering [8]. Each data point of the data set belongs to exactly one cluster in hard clustering. Fuzzy set theory which was proposed by Zadeh [9] in 1965 is used to describe the membership degrees in fuzzy cluster analysis. Therefore, each data point of the data set belongs to two or more clusters with a membership degree between 0 and 1. Due to the capacity of handling uncertainty and vagueness, the potential of fuzzy clustering to reveal the underlying structures in data with regard to similarities or dissimilarities among them can be exploited [10].

One of the widely used methods in fuzzy clustering is Fuzzy C-Means clustering (FCM) [11]. The FCM method attempts to partition a data set into a collection of \( c \) fuzzy groups. It finds a cluster center in each group such that the intra-distance within the group is minimized and the inter-distance between each group is maximized. All of the fuzzy clustering methods that have been applied recently mostly use an extension of the FCM algorithm. As we have discussed before, partitional clustering suffers from the following two drawbacks:

- The number of clusters needs to be specified in advance. Furthermore, it requires prior knowledge or ground truth of the data.
- In most cases data points in overlapping areas can not be categorized correctly.
In order to overcome these two drawbacks, we proposed a fuzzy C-means clustering approach using automated Particle Swarm Optimization (PSO) for clustering analysis. The rest of this paper is organized as follows. In Section II, fuzzy c-means and PSO are introduced. The proposed algorithm is described in Section III. A list of validity indices is given in Section IV. The experimental results and analysis is described in Section V. We finally conclude this paper in Section VI.

II. RELATED WORK

FCM was first developed by [12] in 1973 and was extended by [11] in 1981. Since then, FCM is one of the most promising fuzzy clustering methods. Many variants of FCM have been introduced. For example, the Gustafson-Kessel (GK) algorithm [7] is a fuzzy clustering technique which can estimate local covariance to partition data into subsets that can be well fitted with linear sub-models. However, considering a general structure of the covariance matrix can have substantial effect on the modeling approach, thus the Gath-Geva algorithm [13] was proposed. The fuzzy c-varieties (FCV) [14] clustering algorithm is a fuzzy clustering algorithm where the prototype of each cluster is a multi-dimensional linear vector. It is similar to cluster analysis, however, it uses the statistical method of principal component analysis. A generalized FCM algorithm is presented in [15]. The algorithm proposes an approach for setting the algorithm parameters.

With regards to PSO approaches, two methods called PSO-V and PSOU are introduced in [16]. A reformulated objective function of fuzzy c-means is minimized by PSO for cluster analysis. A PSO-based fuzzy clustering algorithm is introduced to overcome the shortcomings of FCM [17]. An ant colony clustering algorithm is applied for solving clustering problem in [18]. The algorithm employs the global pheromone updating and the heuristic information to find clustering solutions. In [19], a genetic fuzzy K-modes algorithm for clustering categorical data is proposed. The fuzzy K-modes clustering is treated as an optimization problem and a genetic algorithm is used to obtain the global optimal solution. A hybrid data clustering algorithm which makes use of the merits of PSO and KHM is proposed in [20]. The proposed algorithm helps the KHM to escape from local optima. In addition, it overcomes the problem of slow convergence of the PSO algorithm. A hybrid evolutionary algorithm called FAPSO-ACO-K is discussed in [21]. The hybrid algorithm is based on PSO, ACO and k-means applied to cluster analysis. A new method for dynamic parameter adaptation in PSO is proposed in [22]. The proposed algorithm uses fuzzy logic to improve the convergence and diversity of the swarm in PSO.

Although PSO techniques do eventually locate the desired solution, the high computational cost and the slow convergence rate severely limit the use of PSO on clustering analysis. For these reasons, a chaotic map PSO with an accelerated convergence rate strategy is introduced in [23]. The algorithm adopts chaotic maps and adaptive action to avoid entrapment of the PSO in a local optimum. A hybrid fuzzy clustering method based on FCM and FPSO is proposed to overcome the shortcomings of PSO in [24]. A modified version of PSO, known as Multi-Elitist PSO (MEPSO), is proposed in [25]. This approach solves the hard clustering problem which can automatically determine the optimal number of clusters. This approach shows that PSO is guaranteed to solve clustering problem automatically.

III. FUZZY C-MEANS AND PARTICLE SWARM OPTIMIZATION

A. Fuzzy C-means Clustering

Fuzzy clustering is a method of clustering which allows one piece of data to belong to two or more clusters. The FCM algorithm is an iterative partition clustering technique which was first introduced by Dunn [12] and was extended by Bezdek [11]. FCM is a pretty standard least squared error model that generalizes an earlier and very popular non-fuzzy c-means model that produces hard clusters of the data. An optimal c partition is produced iteratively by minimizing the weighted within group sum of squared error objective function:

$$J = \sum_{i=1}^{n} \sum_{j=1}^{c} (u_{ij})^m d^2(y_i, c_j)$$

where $Y = [y_1, y_2, ..., y_n]$ is the data set in a d-dimensional vector space. n is the number of data items. c is the number of clusters which is defined by the user where $2 \leq c \leq n$. $u_{ij}$ is the degree of membership of $y_i$ in the $j^{th}$ cluster. $m$ is a weighted exponent on each fuzzy membership. $c_j$ is the center of cluster $j$. $d^2(x_i, c_j)$ is a square distance measure between object $y_i$ and cluster $c_j$. An optimal solution with c partitions can be obtained via an iterative process which is as follows:

1) Input(c, m, $\epsilon$, data)
2) Initialize the fuzzy partition matrix $U = [u_{ij}]$
3) Iteration starts and set $t=1$
4) Calculate the c cluster centers with $U^t$:

$$c_i = \frac{\sum_{i=1}^{n} (u_{ij})^m y_i}{\sum_{i=1}^{n} (u_{ij})^m}$$  

5) Calculate the membership $U^{t+1}$ using:

$$u_{ij} = \frac{1}{\sum_{k=1}^{c} (\frac{d_{ij}}{d_{ik}})^{\frac{2}{m-1}}}$$

6) If the stopping criteria is not met, $t = t + 1$ and go to Step 4.
B. Particle Swarm Optimization

PSO was originally designed and introduced by Eberhart and Kennedy [26]. The PSO is a population search algorithm which intends to simulate the choreography of a bird flock. Each individual, called particle, within the swarm is represented by a vector in a multidimensional search space. A velocity vector is assigned to each particle to determine the next movement of the particle. Each particle updates its velocity based on the current velocity, best personal position it has explored so far and the global best position explored by the swarm.

The velocity and position of the particle at the next iteration is updated as:

$$V_i(t+1) = wV_i(t)+c_1 r_1 (X_i^1(t) - X_i(t)) + c_2 r_2 (X^g - X_i(t))$$

$$X_i(t + 1) = X_i(t) + V_i(t + 1)$$

for the $i^{th}$ particle, where $w$ is the inertia weight, $V_i(t)$ is the previous velocity in iteration $t$ of $i^{th}$ particle, $c_1$ and $c_2$ are coefficients. Generally, $r_1$ and $r_2$ are random numbers between 0 and 1. $(X_i^1(t) - X_i(t))$ is the difference between the local best $X_i^1$ of the $i^{th}$ particle and the previous position $X_i(t)$. Similarly, $(X^g - X_i(t))$ is the difference between the global best $X^g$ and the previous position $X_i(t)$. 

IV. PROPOSED APPROACH

The proposed algorithm is based on PSO and FCM. The particle encoding, velocity encoding, decoding and clustering validation is described separately. The procedures of the proposed algorithm are presented at the end of this section.

A. Particle Encoding

A particle is a $2 \times k$ matrix, where $k$ is the maximum number of clusters that is predefined. The first row represents the centers. Each value in the second row controls the activation of each center in the first row.

$$X_i = \begin{pmatrix} x_{i,1}^1 & x_{i,2}^1 & \cdots & x_{i,k}^1 \\ t_{i,1}^1 & t_{i,2}^1 & \cdots & t_{i,k}^1 \end{pmatrix}$$

where $x_{i,k}^1$ represents the $i^{th}$ particle’s position in cluster $k$, $x_{i,k}^1$ should be in the range of $[x_{min}, x_{max}]$. $t_{i,k}^1$ is the $i^{th}$ particle’s threshold value in the range of $[0, 1]$. If the threshold value is greater than 0.5, the center is activated. Otherwise, it is deactivated.

B. Velocity Encoding

The velocity matrix should have the same dimension as the position matrix with a range. Suppose we set the range as $[v_{min}, v_{max}]$, all values of the velocity matrix should be between $v_{min}$ and $v_{max}$. Thus, the $i^{th}$ velocity is denoted as:

$$V_i = \begin{pmatrix} v_{i,1,1} \ v_{i,1,2} \ \cdots \ v_{i,1,k} \\ v_{i,2,1} \ v_{i,2,2} \ \cdots \ v_{i,2,k} \end{pmatrix}$$

Similarly, $k$ is the maximum number of clusters. The first row is the velocity of the centers, and the second row is the velocity of the threshold values.

C. Decoding

$Y = (y_1, y_2, \ldots, y_n)$ is the data set with $d$ dimensions. The cluster centers can be decoded as $C = (c_1, c_2, \ldots c_k)$ using Equation 2.

D. Clustering Validation Techniques

The aim of clustering validation is to evaluate the clustering results to find the best partition that fits the underlying data. Thus, cluster validity is used to quantitatively evaluate the result of clustering algorithms. Compactness and separation are considered as two widely used criteria in measuring the quality of partitioning a data set into a number of clusters. Conventional approaches run the algorithm iteratively using different input values and select the best validity measure to determine the “optimum” number of clusters. A collection of validity indices in fuzzy clustering is listed below.

1) Least Squared Error (SE) Index: The weighted within cluster sum of squared error function is used [27]:

$$J_m = \sum_{i=1}^{n} \sum_{j=1}^{c} u_{ij}^m ||y_i - c_j||^2$$

where $y_i$ is the $i^{th}$ data point with $d$ dimensions. $c_j$ is the value of the $j^{th}$ cluster, and $||y_i - c_j||$ is the Euclidean distance between $y_i$ and $c_j$. $J_m$ takes its minimum value when the cluster structure is best.

2) Partition Coefficient (PC) Index: The partition coefficient (PC) is defined as [11]:

$$PC = \frac{1}{n} \sum_{i=1}^{n} \sum_{j=1}^{c} u_{ij}^2$$

PC obtains its maximum value when the cluster structure is optimal.

3) Partition Entropy (PE) Index: The partition entropy was defined as [14]:

$$PE = -\frac{1}{n} \sum_{i=1}^{n} \sum_{j=1}^{c} u_{ij} \log_b(u_{ij})$$

where $b$ is the logarithmic base. PE gets its minimum value when the cluster structure is optimal.

4) Modified Partition Coefficient (MPC) Index: Modification of the PC index, which can reduce the monotonic tendency, is proposed by Dave in 1996 [28].

$$MPC = 1 - \frac{c}{c-1} (1 - PC)$$

where $c$ is the number of cluster. An optimal cluster number is found by maximizing MPC to produce a best clustering performance for a data set.
5) Fukuyama and Sugeno (FS) Index: Fukuyama and Sugeno proposed a validity function in 1989 [29]. It is defined as:

$$FS = \sum_{i=1}^{n} \sum_{j=1}^{c} \mu_{ij}^{m} \|x_i - c_j\| - \sum_{i=1}^{n} \sum_{j=1}^{c} \mu_{ij}^{n} \|c_j - \bar{c}\|$$  \hspace{1cm} (12)

where $\bar{c} = \sum_{j=1}^{c} c_j / c$. It measures the separation. The first term equals to $J_m$ which is the least squared error. It measures the compactness. The best clustering performance for a data set is found by maximizing the value of FS.

6) Xie-Beni (XB) Index: Xie and Beni proposed a validity function in 1991 [30], and later it was modified by Bezdek in 1995 [31].

$$XB = \frac{J_m}{n \times \min_i \sum_j ||z_i - \bar{z}_j||^2}$$  \hspace{1cm} (13)

XB reaches its minimum value when the cluster structure is optimal.

7) Partition Coefficient and Exponential Separation (PCAES) Index: The partition coefficient and exponential separation (PCAES) index [32] is defined as:

$$PCAES = \sum_{i=1}^{n} \sum_{j=1}^{c} \left( \frac{(u_{ij})^2}{u_M} - \frac{c}{k=1} \exp(-\min_{k \neq i} ||z_i - z_k||^2 / \beta_T) \right)$$  \hspace{1cm} (14)

where $u_M = \min_{1 \leq j \leq c} (\sum_{i=1}^{n} u_{ij}^2)$ and $\beta_T = (\sum_{j=1}^{c} ||\bar{z}_j - \bar{z}||^2) / c$. $\bar{z} = \sum_{i=1}^{n} (y_i / n)$. PCAES takes its maximum value when the cluster structure is optimal.

8) Weighted Inter-Intra (Wint) Index: The weighted inter-intra (Wint) measure is introduced by Strehl [33] in 2002. It compares the compactness of the data to its separation.

$$Wint = (1 - \frac{2c}{n})(1 - \frac{\sum_{i} \frac{1}{n-c_i} \sum_{j \neq i} \text{inter}(c_i, c_j)}{\sum_{i} \frac{2}{c_i - 1} \text{intra}(c_i)})$$  \hspace{1cm} (15)

where $\text{intra}(c_i)$ is the average intra-distance within cluster $i$, $\text{inter}(c_i, c_j)$ is the average inter-distance between cluster $i$ and cluster $j$. Wint obtains its maximum value when the cluster structure is optimal.

The procedure of the proposed algorithm is listed below:

**Input:** data set $Y = [y_1, y_2, ..., y_n]$, number of cluster $c$, fuzzification coefficient $m$.

**Output:** a $n \times c$ partition matrix $U$ and corresponding centers.

1) Randomly initialize a swarm
2) Iteration starts and set $t=1$
3) Update the velocity of each particle using Equation 4
4) Update the position of each particle using Equation 5
5) Update the personal best and global best
6) Calculate the partition matrix $U$
7) If the stopping criterion is not met, $t = t + 1$ and go back to Step 3
8) The partition matrix $U$ of the global best is used to reconstruct the original data

9) Calculate the reconstruction error. In order to use a consistent method to evaluate the eight different indices, the reconstruction criterion (RC) [34] is used. The reconstruction criterion uses the cluster prototypes and partition matrix to “reconstruct” the original data vectors. The reconstructed version of the original data vectors, $Y = [\hat{y}_1, \hat{y}_2, ..., \hat{y}_n]$, is calculated as:

$$\hat{y}_i = \frac{\sum_{j=1}^{c} u_{ij}^m c_j}{\sum_{j=1}^{c} u_{ij}^m}$$  \hspace{1cm} (16)

Once the reconstruction has been finished, the squared error of the reconstruction vectors and original vectors are evaluated using Equation 17.

$$E = \sum_{i=1}^{n} ||y_i - \hat{y}_i||^2$$  \hspace{1cm} (17)

10) Select the partition matrix and centers corresponding to the minimum reconstruction error.

V. EXPERIMENTS AND RESULTS

In this section, the experimental setup, datasets and experimental study are described.

A. Experimental Setup

The experiments are implemented and evaluated on an ASUS desktop (Intel(R) Dual Core I3 CPU @3.07 GHz, 3.07 GHz) Matlab Version 7.13. All measurements of the proposed algorithm are tested 30 times. The parameters required for the proposed algorithm are listed in Table I.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
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<tbody>
<tr>
<td>Maximum number of cluster</td>
<td>10</td>
</tr>
<tr>
<td>Maximum iteration</td>
<td>50</td>
</tr>
<tr>
<td>Swarm size</td>
<td>25</td>
</tr>
<tr>
<td>Maximum run</td>
<td>30</td>
</tr>
<tr>
<td>Fuzzification coefficient (m)</td>
<td>2</td>
</tr>
</tbody>
</table>

Table I: Parameters and their values of the proposed algorithm.

B. Datasets

The experiments are conducted on a number of datasets taken from the UCI repository [35], and one synthetic data set was generated in Matlab. The datasets are described in Table II.

<table>
<thead>
<tr>
<th>Data Set</th>
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<th>Instances</th>
<th>Classes</th>
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<td>Iris</td>
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<td>150</td>
<td>3</td>
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</tbody>
</table>

Table II: Datasets used for the experiments.
C. Experimental Study

1) Use of Synthetic Data: In order to investigate the clustering performance with different numbers of clusters, we use a synthetic data set to test the clustering performance using K-means, FCM and the proposed algorithm (FPSO). K-means and FCM are the default methods in Matlab. The data generated is shown in Figure 1. A toolbox for estimating the number of clusters implemented by Kaijun Wang is adopted. Nine traditional indices, Rand [36], Mirkin [37], Hubert [38], Silhouette [39], Davies-Bouldin [40], Calinski-Harabasz [41], Krzanowski-Lai [42], Hartigan [43] and Homogeneity-Separation [44] are implemented as used by Wang.

Figure 2 lists the performance of the synthetic data set using K-means. The Rand index measures an agreement of the clustering results. As the number of clusters increases, the agreement of the clustering results decrease. As the number of clusters increases, the performance using Mirkin distance increases. Hubert index has the same performance as Rand index. As the number of clusters increases, the performance using Silhouette improves. The optimal cluster numbers found by Davies-Bouldin, Calinski-Harabasz, Krzanowski-Lai, Hartigan and Homogeneity-Separation are 2, 6, 9, 1, and 2, respectively.

Figure 3 shows the performance results using FCM on the same synthetic data set. As shown in the figure, Rand, Mirkin, Hubert and Silhouette have the same performance as K-means. The optimal number of clusters found by Davies-Bouldin, Calinski-Harabasz, Krzanowski-Lai, Hartigan and Homogeneity-Separation are 9, 7, 4, 1, and 2, respectively.

Due to the stochastic nature of our proposed algorithm, we tested the proposed algorithm on 30 runs and calculated the average optimal number of clusters as listed in Table IV. The values in parenthesis are the standard deviation. The results show that the proposed algorithm can obtain an optimal cluster number except for the Breast data set which returns \( c = 3 \) using the MPC index.

Table IV: Eight different indices using the proposed algorithm.

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True Class labels 2 2 2 2 3

VI. CONCLUSION

In this study, we proposed an algorithm based on PSO and FCM in order to overcome the drawbacks of traditional partition clustering. The proposed algorithm uses a threshold vector to control the number of clusters and solves the clustering problem via an iterative fuzzy partition process. We generated a synthetic dataset and used 6 datasets from the UCI repository. The results show that the proposed algorithm can automatically find the optimal number of clusters.

In Table III, the reconstruction errors of the transfusion data set, where \( c \) ranges from 2 to 9, have been calculated using the proposed algorithm by applying Equations 8-15. As shown by the results, the bold values are minimum reconstruction errors with different cluster numbers for each measure. 6 out of 8 cases show that \( c = 2 \) is the optimal number of clusters.

Table III: Reconstruction error with varying \( c \) using transfusion data set.

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<td>23.6</td>
<td>43.0</td>
<td>25.1</td>
<td>36.1</td>
<td>27.1</td>
<td>61.3</td>
<td>68.8</td>
<td>63.1</td>
</tr>
<tr>
<td>PCAES</td>
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<td>81.7</td>
<td>82.5</td>
<td>48.1</td>
<td>53.8</td>
<td>57.5</td>
<td>97.2</td>
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<tr>
<td>Wint</td>
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<td>29.3</td>
<td>25.4</td>
<td>47.4</td>
<td>51.5</td>
<td>68.8</td>
<td>42.5</td>
<td>36.5</td>
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</table>
However, due to the slow convergence and the stochastic nature of the PSO algorithm, the prediction results of a single run fluctuates and is thus hard to make predictions. Unlike K-means and FCM, the proposed algorithm need to be tested repeatedly in order to find the optimal solution. In addition, the maximum number of clusters is predefined, and the recursive increase of the number of clusters is computational expensive.

As for future work, it would be interesting to improve the proposed algorithm to achieve more stable predictions with fewer runs. Moreover, we are planning to explore the proposed algorithm with big datasets, and therefore parallelization techniques are necessary.

REFERENCES


Figure 3: FCM using 9 different validity indices
Figure 4: FPSO using 9 different validity indices


